

GEORGIA'S K-12 MATHEMATICS STANDARDS 2021

Algebra:

Concepts & Connections (HS Course 1)

MATHEMATICS KEY COMPETENCIES & COURSE STANDARDS WITH LEARNING OBJECTIVES IN PROGRESSION ORDER



GEORGIA'S K-12 MATHEMATICS STANDARDS 2021

Governor Kemp and Superintendent Woods are committed to the best set of academic standards for Georgia's students – laying a strong foundation of the fundamentals, ensuring age- and developmentally appropriate concepts and content, providing instructional supports to set our teachers up for success, protecting and affirming local control and flexibility regarding the use of mathematical strategies and methods, and preparing students for life. These Georgia-owned and Georgia-grown standards leverage the insight, expertise, experience, and efforts of thousands of Georgians to deliver the very best educational experience for Georgia's 1.7 million students.

In August 2019, Governor Brian Kemp and State School Superintendent Richard Woods announced the review and revision of Georgia's K-12 mathematics standards. Georgians have been engaged throughout the standards review and revision process through public surveys and working groups. In addition to educator working groups, surveys, and the Academic Review Committee, Governor Kemp announced a new way for Georgians to provide input on the standards: the Citizens Review Committee, a group composed of students, parents, business and community leaders, and concerned citizens from across the state. Together, these efforts were undertaken to ensure Georgians will have buy-in and faith in the process and product.

The Citizens Review Committee provided a charge and recommendations to the working groups of educators who came together to craft the standards, ensuring the result would be usable and friendly for parents and students in addition to educators. More than 14,000 Georgians participated in the state's public survey from July through September 2019, providing additional feedback for educators to review. The process of writing the standards involved more than 200 mathematics educators -- from beginning to veteran teachers, representing rural, suburban, and metro areas of our state.

Grade-level teams of mathematics teachers engaged in deep discussions; analyzed stakeholder feedback; reviewed every single standard, concept, and skill; and provided draft recommendations. To support fellow mathematics teachers, they also developed learning progressions to show when key concepts were introduced and how they progressed across grade levels, provided examples, and defined age/developmentally appropriate expectations.

These teachers reinforced that strategies and methods for solving mathematical problems are classroom decisions -- not state decisions -- and should be made with the best interest of the individual child in mind. These recommended revisions have been shared with the Academic Review Committee, which is composed of postsecondary partners, age/development experts, and business leaders, as well as the Citizens Review Committee, for final input and feedback.

Based on the recommendation of Superintendent Woods, the State Board of Education will vote to post the draft K-12 mathematics standards for public comment. Following public comment, the standards will be recommended for adoption, followed by a year of teacher training and professional learning prior to implementation.

Algebra: Concepts & Connections

Overview

This document contains a draft of Georgia's 2021 K-12 Mathematics Standards for the High School Algebra: Concepts and Connections Course, which is the first course in the high school course sequence.

The standards are organized into big ideas, course competencies/standards, and learning objectives/expectations. The grade level key competencies represent the standard expectation of learning for students in each grade level. The competencies/standards are each followed by more detailed learning objectives that further explain the expectations for learning in the specific grade levels.

New instructional supports are included, such as clarification of language and expectations, as well as detailed examples. These have been provided for teaching professionals and stakeholders through the Evidence of Student Learning Column that accompanies each learning objective.

Course Description:

This course is designed as the first course in a three-course series. Students will apply their algebraic and geometric reasoning skills to make sense of problems involving algebra, geometry, bivariate data, and statistics. This course focuses on algebraic, quantitative, geometric, graphical, and statistical reasoning. In this course, students will continue to enhance their algebraic reasoning skills when analyzing and applying a deep understanding of linear functions, sums and products of rational and irrational numbers, systems of linear inequalities, distance, midpoint, slope, area, perimeter, nonlinear equations and functions, quadratic expressions, equations and functions, exponential expressions, equations, and functions, and statistical reasoning.

High school course content standards are listed by big ideas including Data and Statistical Reasoning, Probabilistic Reasoning, Functional and Graphical Reasoning, Patterning and Algebraic Reasoning, and Geometry Patterning and Spatial Reasoning.

Prerequisite:

This course is designed for students who have successfully completed Kindergarten through 8th grade mathematics.

Georgia's K-12 Mathematics Standards - 2021 Mathematics Big Ideas and Learning Progressions, High School

Mathematics Big Ideas, HS

HIGH SCHOOL
MATHEMATICAL PRACTICES (MP)
MATHEMATICAL MODELING (MM)
NUMERICAL REASONING (NR)
PATTERNING & ALGEBRAIC REASONING (PAR)
FUNCTIONAL & GRAPHICAL REASONING (FGR)
GEOMETRIC & SPATIAL REASONING (GSR)
DATA & STATISTICAL REASONING (DSR)
PROBABILISTIC REASONING (PR)

The 8 Mathematical Practices and the Mathematical Modeling Framework are essential to the implementation of the content standards presented in this course. More details related to these concepts can be found in the links below and in the first two standards presented in this course:

Mathematical Practices

Mathematical Modeling Framework

Algebra: Concepts & Connections

The eleven course standards listed below are the key content competencies students will be expected to master in this course.

Additional clarity and details are provided through the classroom-level learning objectives and evidence of student learning details for each course standard found on subsequent pages of this document.

COURSE STANDARDS

A.MP: Display perseverance and patience in problem-solving. Demonstrate skills and strategies needed to succeed in mathematics, including critical thinking, reasoning, and effective collaboration and expression. Seek help and apply feedback. Set and monitor goals.

A.MM.1: Apply mathematics to real-life situations; model real-life phenomena using mathematics.

A.FGR.2: Construct and interpret arithmetic sequences as functions, algebraically and graphically, to model and explain real-life phenomena. Use formal notation to represent linear functions and the key characteristics of graphs of linear functions, and informally compare linear and non-linear functions using parent graphs.

A.GSR.3: Solve problems involving distance, midpoint, slope, area, and perimeter to model and explain real-life phenomena.

A.PAR.4: Create, analyze, and solve linear inequalities in two variables and systems of linear inequalities to model real-life phenomena.

A.NR.5: Investigate rational and irrational numbers and rewrite expressions involving square roots and cube roots.

A.PAR.6: Build quadratic expressions and equations to represent and model real-life phenomena; solve quadratic equations in mathematically applicable situations.

A.FGR.7: Construct and interpret quadratic functions from data points to model and explain real-life phenomena; describe key characteristics of the graph of a quadratic function to explain a mathematically applicable situation for which the graph serves as a model.

A.PAR.8: Create and analyze exponential expressions and equations to represent and model real-life phenomena; solve exponential equations in mathematically applicable situations.

A.FGR.9: Construct and analyze the graph of an exponential function to explain a mathematically applicable-situation for which the graph serves as a model; compare exponential with linear and quadratic functions.

A.DSR.10: Collect, analyze, and interpret univariate quantitative data to answer statistical investigative questions that compare groups to solve real-life problems; Represent bivariate data on a scatter plot and fit a function to the data to answer statistical questions and solve real-life problems.

Algebra: Concepts & Connections

MATHEMA	TICAL MODELING		
A.MM.1: A	pply mathematics to real-life situations; model real-life	phenomena using mathema	atics.
	Expectations		ce of Student Learning e; see Course Overview for more details)
A.MM.1.1	Explain applicable, mathematical problems using a mathematical model.	 framework of real-life probler Mathematically applicable proframework makes sense, realler 	I with opportunities to learn mathematics in the ms. oblems are those presented in which the given alistically and mathematically, and allows for students to be solve the problem (model with mathematics).
A.MM.1.2	Create mathematical models to explain phenomena that exist in the natural sciences, social sciences, liberal arts, fine and performing arts, and/or humanities domains.	Fundamentals	se the content learned in this course to create a
A.MM.1.3	Use units of measure (linear, area, capacity, rates, and time) as a way to make sense of conceptual problems; identify, use, and record appropriate units of measure within the given framework, within data displays, and on graphs; convert units and rates using proportional reasoning given a conversion factor; use units within multi-step problems and formulas; interpret units of input and resulting units of output.	Strategies and Methods Dimensional analysis may be used when converting units and rates.	Units of measure may include linear, area, capacity, rates, and time.
A.MM.1.4	Use various mathematical representations and structures with this information to represent and solve real-life problems.	that are presented numerical	uently navigate between mathematical representations lly, algebraically, and graphically. s, students should be given opportunities to analyze bhing technologies.
A.MM.1.5	Define appropriate quantities for the purpose of descriptive modeling.		a, or problem, students should be able to determine, quantities for representing the situation.

FUNCTION	AL & GRAPHICAL REASONING – function	on notation, modeling linear functions, linear vs. nonlinear col	mparisons
		nces as functions, algebraically and graphically, to mod	
		ar functions and the key characteristics of graphs of line	ar functions, and informally
compare li	near and non-linear functions using par		
	Expectations	Evidence of Student Learni	
A 500 0 4	I lea math amatically applicable city ations	(not all inclusive; see Course Overview for mor	
A.FGR.2.1	Use mathematically applicable situations algebraically and graphically to build and interpret arithmetic sequences as functions whose domain is a subset of the integers.	Students should be able to: make connections between linear functions and arithmetic sequences presented in mathematically applicable-situations. build and interpret arithmetic sequences as functions presented graphically and algebraically. convert arithmetic sequences from explicit to recursive form and vice versa. define sequences recursively and explicitly.	 ■ By graphing or calculating terms, students should be able to show how the arithmetic sequence in recursive form a₁=7, a_n=a_{n-1} +2; the arithmetic sequence in explicit form a_n = 2(n-1) + 7; and the function f(x) = 2x + 5 (when x is a natural number) all define the same sequence.
A.FGR.2.2	Construct and interpret the graph of a linear function that models real-life phenomena and represent key characteristics of the graph using formal notation.	 Strategies and Methods Students should be able to use graphs created by hand and with technology, verbal descriptions, tables, and function notation when analyzing linear functions that represent real-life phenomena. Students should be given opportunities to use interactive graphing technologies to explore and analyze key characteristics of linear functions, including domain, range, intercepts, intervals where the function is increasing or decreasing, positive or negative, maximums and minimums over a specified interval, and end behavior. 	Students should be able to express characteristics in interval and set notation with linear functions. Students should be able
A.FGR.2.3	Relate the domain and range of a linear function to its graph and, where applicable, to the quantitative relationship it describes. Use formal interval and set notation to describe the domain and range of linear functions.	 Examples If the function h(n) gives the number of hours it takes a person to as the set of positive integers would be an appropriate domain for the ference of the set of positive integers would be an appropriate domain for the ference of the set of positive integers would be an appropriate domain for the ference of the set of the s	semble n engines in a factory, then unction.
A.FGR.2.4	Use function notation to build and evaluate linear functions for inputs in their domains and interpret statements that use function	Student should develop a deep understanding of function notation to functions; this understanding will be applied to other functions studies.	

	notation in terms of a mathematical framework.	Students should be able to interpret the domain walgebraically, and graphically.	when given a function expressed numerically,
A.FGR.2.5	Analyze the difference between linear functions and nonlinear functions by informally analyzing the graphs of various parent functions (linear, quadratic, exponential, absolute value, square root, and cube root parent curves).	 Fundamentals Students should explore the parent function graphs to compare linear and nonlinear relationships (including a visual analysis of end behavior, increasing and decreasing, domain and range, intercepts, and general curvature). Learning all the characteristics of these nonlinear functions is not an expectation for this learning objective. Students should be able to identify parent functions by name (i.e., linear, quadratic, etc.). Students should have opportunities to explore the various graphs using technology. 	 Strategies and Methods Students should be able to informally analyze the curvature of several parent functions to highlight the characteristics of linear functions in comparison to several nonlinear functions. This is an introduction to functions they will explore in future units and courses. Student should be provided opportunities to utilize graphing calculators and interactive graphing technologies to explore this concept.

GEOMETR	IC & SPATIAL REASONING – distance,	midpoint, slope, area, and perimeter	
A.GSR.3: S	Solve problems involving distance, mic	lpoint, slope, area, and perimeter to model and explain real-life p	henomena.
	Expectations	Evidence of Student Learning	
	LApeciations	(not all inclusive; see Course Overview for more details)	
A.GSR.3.1	Solve real-life problems involving slope, parallel lines, perpendicular lines, area, and perimeter.	 Fundamentals Students should apply their understanding of linear relationships to solve real-li related to slope, parallel lines, perpendicular lines, area, and perimeter. Students should be able to calculate the area and perimeter of special parallelo simple, unknown side lengths. 	
A. GSR.3.2	Apply the distance formula, midpoint formula, and slope of line segments to solve real-world problems.	 Fundamentals Students should be able to apply their understanding of slope and use the distance and midpoint formulas to solve real-world problems. In a real-life application, using a figure in the coordinate plane, students should be able to find a location using distance or midpoint. 	Find the distance of a line segment plotted on the coordinate plane.

	Create, analyze, and solve linear inequal	inequalities and systems of linear inequalities ities in two variables and systems of linear i	nequalities to model real-life
	Expectations	Evidence of Stu	
A.PAR.4.1	Create and solve linear inequalities in two variables to represent relationships between quantities including mathematically applicable situations; graph inequalities on coordinate axes with labels and scales.	 (not all inclusive; see Course Fundamentals) Students should be given the opportunity to explore the difference between solid lines and dashed lines through exploration on an interactive graph. Students should have had opportunities to create an solve linear equations and inequalities throughout middle school mathematics. Students should recognize that the graph of a linear inequality in two variables is a half-plane. 	Strategies and Methods When necessary, students should be able to rewrite the inequality in various forms, such as slope-intercept form, for graphing. Students should be given opportunities to solve linear inequalities and algebraically. These linear inequalities
A.PAR.4.2	Represent constraints of linear inequalities and interpret data points as possible or not possible.	 Terminology Possible data points are solutions to the inequality or inequalities; data points that are not possible are non-solutions to the inequality or inequalities. 	
A.PAR.4.3	Solve systems of linear inequalities by graphing, including systems representing a mathematically applicable situation.	Fundamentals Ensure constraints are represented. Students in Grade 8 mathematics modeled with and solved systems of linear equations to solve real-life problems.	Strategies and Methods Students should be provided opportunities to use technology tools to solve systems of linear inequalities graphically.

NUMERICA	AL REASONING - rational and irrational nu	umbers, square roots and cube roots	
A.NR.5: Inv	estigate rational and irrational number	s and rewrite expressions involving square roots a	nd cube roots.
	Expectations	Evidence of Student Learning	
		(not all inclusive; see Course Overview for more details)	
A.NR.5.1	Rewrite algebraic and numeric expressions involving radicals.	Relevance and Application Students should be able to use the operations of addition, su within expressions limited to square roots and cube roots.	btraction, and multiplication, with radicals
A.NR.5.2	Using numerical reasoning, show and explain that the sum or product of rational numbers is rational, the sum of a rational number and an irrational number is irrational, and the product of a nonzero rational number and an irrational number is irrational.	 Fundamentals The tasks selected should aid students with their development of a conceptual understanding of the sums and products of rational and irrational numbers through exploration and investigation. Students should be able to judge the reasonableness of an answer based on their understanding of rational and irrational numbers. 	 Examples Students should know that adding two irrational numbers, such as 3√5 and √7, may result in an irrational number. The side length of a square is√8. Is the perimeter a rational or irrational number?

PATTERNIN	IG & ALGEBRAIC REASONING – quadra	tic expressions & equations	
	uild quadratic expressions and equation ally applicable situations.	ns to represent and model real-life phenomena; solve quadratic equations in	
	Expectations	Evidence of Student Learning (not all inclusive; see Course Overview for more details)	
A.PAR.6.1	Interpret quadratic expressions and parts of a quadratic expression that represent a quantity in terms of its context.	 Fundamentals Students should be able to interpret parts of an expression, such as terms, factors, leading coefficient, coefficients, constant and degree in context. Given mathematically applicable situations which utilize formulas or expressions with multiple terms and/or factors, students should be able to interpret the meaning of given individual terms or factors. 	
A.PAR.6.2	Fluently choose and produce an equivalent form of a quadratic expression to reveal and explain properties of the quantity represented by the expression.	 Students should be able to multiply variable expressions involving the product of a monomial and a binomial and the product of two binomials to produce a quadratic expression. Polynomial operations are included with this objective. Polynomial sums, differences, and products should not exceed a maximum degree of 2. Strategies and Methods Students should be able to move fluently (flexibly, accurately, efficiently) between different forms of a quadratic expression (standard, vertex, and factored forms). Students should be able to move fluently (flexibly, accurately, efficiently) between different forms of a quadratic expression (standard, vertex, and factored forms). Students should be able to move fluently (flexibly, accurately, efficiently) between different forms of a quadratic expression (standard, vertex, and factored forms). 	
A.PAR.6.3	Create and solve quadratic equations in one variable and explain the solution in the framework of applicable phenomena.	 Fundamentals Students should be able to multiply variable expressions involving the product of a monomial and a binomial and the product of two binomials to solve a quadratic equation. Strategies and Methods Students should be able to solve quadratic equatratic (flexibly, accurately, efficiently) by inspection, taking square roots, factoring, completing the square, and applying the quadratic formula, as appropriate to the initial form of the equation. Students should be able to fluently transform a quadratic equation in x into an equation of the form (x − p)² = q that has the same solutions. Students should be able to analyze and explain what the zeros describe in context. 	
A.PAR.6.4	Represent constraints by quadratic equations and interpret data points as possible or not possible in a modeling	 Terminology Possible data points are solutions to the equation(s); data points that are not possible are non-solutions to the equation(s). 	

framework.

FUNCTIONAL & GRAPHICAL REASONING – quadratic functions

A.FGR.7: Construct and interpret quadratic functions from data points to model and explain real-life phenomena; describe key characteristics of the graph of a quadratic function to explain a mathematically applicable situation for which the graph serves as a model.

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	Expectations		Evidence of Student Learr	
A.FGR.7.1	Use function notation to build and evaluate quadratic functions for inputs in their domains and interpret statements that use function notation in terms of a given framework.	build, evaluate, and interpret	 Students should apply their understanding of function notation from their work with linear functions to build, evaluate, and interpret quadratic functions using function notation. Students should be able to interpret the domain given a function expressed numerically, algebraicall 	
A.FGR.7.2	Identify the effect on the graph generated by a quadratic function when replacing $f(x)$ with $f(x) + k$, $kf(x)$, $f(kx)$, and $f(x + k)$ for specific values of k (both positive and negative); find the value of k given the graphs.	 Strategies and Methods Students should be given opportunities to experiment with cases and illustrate an explanation of the effects on the graph using technology. 		and illustrate an explanation of the
A.FGR.7.3	Graph and analyze the key characteristics of quadratic functions.	 Strategies and Methods Students should be able to use verbal descriptions, tables, and graphs created using interactive technology tools. Students should be able to sketch a graph showing key features including domain, range, and intercepts; intervals where the function increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; asymptotes; end behavior. Key characteristics of the quadratic functions should be expressed in interval and set-builder notation using inequalities. 		rcepts; intervals where the function is or negative; relative maximums and es; end behavior. ic functions should be expressed in
A.FGR.7.4	Relate the domain and range of a quadratic function to its graph and, where applicable, to the quantitative relationship it describes.	 Examples If the function h(t) gives the path of a projectile over time, t, then the set of non-negative real numbers would be an appropriate domain for the function because time does not include negative values. A bird is building a nest in a tree 36 feet above the ground. The bird drops a stick from the nest. The function f(x) = -16x² + 36 describes the height of the stick in feet after x seconds. Graph this function. Identify the domain and range of this function. (A student should be able to determine that the appropriate values for the domain and range of this graph are 0 ≤ x ≤ 1.5 and 0 ≤ y ≤ 36, respectively 		es not include negative values. rd drops a stick from the nest. The fter x seconds. Graph this function. the able to determine that the
A.FGR.7.5	Rewrite a quadratic function representing a mathematically applicable situation to reveal the maximum or minimum value of the function it defines. Explain what the value describes in context.	Students should be able to interpret the maximum and minimum value of a quadratic function expressed in a variety of ways.	Strategies and Methods • Students should be able to use interactive graphing technologies to make sense of the maximum and minimum values in context.	Consider the path of a football thrown through the air. When does the football reach its maximum height? How high does the football reach?

A.FGR.7.6	Create quadratic functions in two variables to represent relationships between quantities; graph quadratic functions on the coordinate axes with labels and scales.			ng technologies to make sense hematically applicable situation	
A.FGR.7.7	Estimate, calculate, and interpret the average rate of change of a quadratic function and make comparisons to the average rate of change of linear functions.	graph. • Students should be all over equal intervals a constant rate per unit compare this behavio functions. This can be		ons grow by equal differences hich one quantity changes at a Students should be able to of change of quadratic with a table showing	Strategies and Methods • Functions can be presented symbolically, as a graph, or as a table.
A.FGR.7.8	Write a function defined by a quadratic expression in different but equivalent forms to reveal and explain different properties of the function.	Strategies and Methods Students should be able to move fluently (flexibly, accurately, efficiently) between the factored form, vertex form, and standard form of a quadratic function.	Fundamentals Students should be able to examine a quadratic function by analyzing the zeros, extreme values, and symmetry of the graph and interpret these properties in context.	Strategies and Methods Students should be given opportunities to use a variety of strategies and methods to make sense of the properties of quadratic functions: Factoring Completing the square Quadratic formula Graphing Taking square roots	should be able to compare quadratic functions in standard, vertex, and intercept forms.
A.FGR.7.9	Compare characteristics of two functions each represented in a different way.	algebraically, graphica Students should be al compare a quadranother quadratio compare key cha key characteristic observe using graphical	atic function to a linear function. cracteristics of quadratic functions of linear functions. aphs and tables that a quantieventually exceed a portion	tion, or ctions with the tity increasing	raph of one quadratic nd an algebraic for another, students able to determine the larger maximum. The raph of one function gebraic equation for students should be able ine which has the larger

PATTERNING & ALGEBRAIC REASONING – exponential expressions and equations

A.PAR.8: Create and analyze exponential expressions and equations to represent and model real-life phenomena; solve exponential equations in mathematically applicable situations.

	Expectations	Evidence of Student Learning (not all inclusive; see Course Overview for more details)
A.PAR.8.1	Interpret exponential expressions and parts of an exponential expression that represent a quantity in terms of its framework.	 Fundamentals Students should be able to interpret parts of an expression, such as terms, factors, leading coefficient, coefficients, constant and degree in context. Given mathematically applicable situations which utilize formulas or expressions with multiple terms and/or factors, students should be able to interpret the meaning in context of individual terms or factors.
A.PAR.8.2	Create exponential equations in one variable and use them to solve problems, including mathematically applicable situations.	Relevance and Application Exponential equations are limited to those containing like bases, or exponential equations that could easily be transferred to like bases with linear operations.
A.PAR.8.3	Create exponential equations in two variables to represent relationships between quantities, including in mathematically applicable situations; graph equations on coordinate axes with labels and scales.	Example Exponential growth and decay situations are an expectation for this learning objective.
A.PAR.8.4	Represent constraints by exponential equations and interpret data points as possible or not possible in a modeling environment.	 Terminology Possible data points are solutions to the equation(s); data points that are not possible are non-solutions to the equation(s).

FUNCTIONAL & GRAPHICAL REASONING – exponential functions
A.FGR.9: Construct and analyze the graph of an exponential function to

to explain a mathematically applicable situation for which the

graph se	graph serves as a model; compare exponential with linear and quadratic functions.				
Expectations		Evidence of Student Learning			
		(not all inclusive; see Course Overview for more details)			
A.FGR.9.1	Use function notation to build and evaluate exponential functions for inputs in their domains and interpret statements that use function notation in terms of a context.	 Fundamentals Students should apply their understanding of function notation from their work with linear and quadratic functions to build, evaluate, and interpret exponential functions using function notation. Students should be able to interpret the domain given a function expressed numerically, algebraically, and graphically. 			
A.FGR.9.2	Graph and analyze the key characteristics of simple exponential functions based on mathematically applicable situations.	 Examples If the function, h(n), gives the number of person-hours it takes to assemble n engines in a factory, then the positive integers would be an appropriate domain for the function. The function can be presented symbolically, as a graph, or as a table. Students should be able to estimate the rate of change from a graph. 			

		 Students should be able to sketch a graph of an exponential function sidomain, range, intercepts, average rate of change, intervals where the positive, or negative; relative maximums and minimums; symmetries; a Students should be given opportunities to show that linear functions greexponential functions grow by equal factors over equal intervals. This with a table showing differences, or by calculating average rates of chast should be able to precisely use verbal descriptions, tables, are using technology. Students should be able to create graphs by hand and using graphing to calculator or online interactive graphing technology) 	function is increasing, decreasing symptotes; end behavior. by by a constant rate and that an be shown by algebraic proof onge over equal intervals. d graphs created by hand and echnology (i.e., graphing	of,
		 Students should be able to accurately express characteristics in intervalusing inequalities. 	i notation and set-builder notat	tion
A.FGR.9.3	Identify the effect on the graph generated by	Strategies and Methods		
	an exponential function when replacing $f(x)$ with $f(x) + k$, and k $f(x)$, for specific values of k (both positive and negative); find the value of k given the graphs.	Students should be given opportunities to experiment with cases and ill on the graph using interactive technology.	ustrate an explanation of the e	effects
A.FGR.9.4	algebraically and graphically to build and interpret geometric sequences as functions whose domain is a subset of the integers.	 Fundamentals Sequences can be defined recursively and explicitly. Connections should be made between exponential functions and geometric sequences. The focus of this learning objective is on building and interpreting geometric sequences. Students should be able to covert geometric sequences from explicit form to recursive and vice versa. Students should have ample opportunities to compare geometric sequences with arithmetic sequences presented in a variety of ways. 	■ By graphing or calculatin terms, students should be able to show how the geometric sequence in recursive form a₁=8, a₂=2 1; the geometric sequence explicit form s₂ = 8(2)²-1; the function f(x) = 4(2)x (when x is a natural num all define the same sequence.	2a _n - nce in and
A.FGR.9.5	Compare characteristics of two functions each	Fundamentals	Example	
	represented in a different way.	 Students should be able to present functions algebraically, graphically, numerically in tables, or by verbal descriptions. Students should be able to compare an exponential function to a linear quadratic function, or to another exponential function. Students should be able to compare key characteristics of exponential the key characteristics of linear and quadratic functions. Students should be able to observe using graphs and tables that a qua increasing quadratically will eventually exceed a portion of a quantity in linearly. Students should be able to observe using graphs and tables that a qua increasing exponentially will eventually exceed a portion of a quantity in linearly or quadratically. 	function, a graph of functions an algeb for anoth determin creasing which hat the large intercept	f one and oraic ion her, ne as er y-

DATA & STATISTICAL REASONING – univariate data and single quantitative variables; bivariate data

A.DSR.10: Collect, analyze, and interpret univariate quantitative data to answer statistical investigative questions that compare groups to solve real-life problems; Represent bivariate data on a scatter plot and fit a function to the data to answer statistical questions and solve real-life problems.

solve real-life problems.				
Expectations		Evidence of Student Learning (not all inclusive; see Course Overview for more details)		
A.DSR.10.1	Use statistics appropriate to the shape of the data distribution to compare and represent center (median and mean) and variability (interquartile range, standard deviation) of two or more distributions by hand and using technology.	 Terminology Measures of center include the median a Measures of spread include the range, ir range and standard deviation. Univariate data involves describing a sing such as the age of a student or the height Bivariate data involves relationships between variables, such as comparing the age of their height. 	mean absolute deviation (MAD) learned in sixth grade to interpret the meaning of standard deviation. • Students were first introduced to the concept of MAD as a tool for comparing variability of multiple data sets in sixth grade mathematics. • Students should initially have opportunities to explore standard deviation, by hand, with small data sets, to gain conceptual understanding. • Students should advance to using technology to determine standard deviation to solve problems and answers statistical investigative questions.	
A.DSR.10.2	Interpret differences in shape, center, and variability of the distributions based on the investigation, accounting for possible effects of extreme data points (outliers).	 Strategies and Methods Use the 1.5 IQR rule to determine the outliers and analyze their effects on the data set. 	 Using the 1.5 IQR rule on data set {5,7,8,10,11,12,30}, 30 is determined to be an outlier since it is greater than 19.5, which is the 1.5*IQR +12 (the Q3). 	
A.DSR.10.3	Represent data on two quantitative variables on a scatter plot and describe how the variables are related.	Students should be able to describe the association between two quantitative variations.	direction, strength, and form (linear, non-linear) of the riables.	
A.DSR.10.4	Interpret the slope (predicted rate of change) and the intercept (constant term) of a linear model based on the-investigation of the data.	data and make sense of the slope (pred	ity to utilize interactive graphing technologies to model linear dicted rate of change) visually.	
A.DSR.10.5	Calculate the line of best fit and interpret the correlation coefficient, r , of a linear fit using technology. Use r to describe the strength of the goodness of fit of the regression. Use the linear function to make predictions and	Strategies and Methods Students should be given the opportunity utilize interactive graphing technologies t interpret the correlation coefficient, r.		

	assess how reasonable the prediction is in context.	
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A.DSR.10.6	Decide which type of function is most	Fundamentals
	appropriate by observing graphed data.	Students should be able to emphasize linear, quadratic, and exponential models.
A.DSR.10.7	Distinguish between correlation and	Application and Relevance
	causation.	It is important for students to discover and understand that strong association does not indicate
		causation.

ESSENTIAL INSTRUCTIONAL GUIDANCE

MATHEMATICAL PRACTICES

The Mathematical Practices describe the reasoning behaviors students should develop as they build an understanding of mathematics – the "habits of mind" that help students become mathematical thinkers. There are eight standards, which apply to all grade levels and conceptual categories.

These mathematical practices describe how students should engage with the mathematics content for their grade level. Developing these habits of mind builds students' capacity to become mathematical thinkers. These practices can be applied individually or together in mathematics lessons, and no particular order is required. In well-designed lessons, there are often two or more Standards for Mathematical Practice present.

MATHEMATICAL PRACTICES		
A.MP: Display perseverance and patience in problem-solving. Demonstrate skills and strategies needed to succeed in mathematics, including critical thinking, reasoning, and effective collaboration and expression. Seek help and apply feedback. Set and monitor goals.		
Code	Expectation	
A.MP.1	Make sense of problems and persevere in solving them.	
A.MP.2	Reason abstractly and quantitatively.	
A.MP.3	Construct viable arguments and critique the reasoning of others.	
A.MP.4	Model with mathematics.	
A.MP.5	Use appropriate tools strategically.	
A.MP.6	Attend to precision.	
A.MP.7	Look for and make use of structure.	
A.MP.8	Look for and express regularity in repeated reasoning.	

MATHEMATICAL MODELING

Teaching students to model with mathematics is engaging, builds confidence and competence, and gives students the opportunity to collaborate and make sense of the world around them, the main reason for doing mathematics. For these reasons, mathematical modeling should be incorporated at every level of a student's education. This is important not only to develop a deep understanding of mathematics itself, but more importantly to give students the tools they need to make sense of the world around them. Students who engage in mathematical modeling will not only be prepared for their chosen career but will also learn to make informed daily life decisions based on data and the models they create.

The diagram below is a mathematical modeling framework depicting a cycle of how students can engage in mathematical modeling when solving a real-life problem or task.

A Mathematical Modeling Framework **Explore & describe real**life, mathematical situations or problems. Evaluate the model and Gather information, make Critical thinking interpret solutions assumptions, and define Communication generated from other variables related to the models. Draw and validate Collaboration problem. conclusions. **Creative Problem** Solving Analyze and revise models, at a solution to explain the as necessary.

Image adapted from: Suh, Matson, Seshaiyer, 2017

FRAMEWORK FOR STATISTICAL REASONING

Statistical reasoning is important for learners to engage as citizens and professionals in a world that continues to change and evolve. Humans are naturally curious beings and statistics is a language that can be used to better answer questions about personal choices and/or make sense of naturally occurring phenomena. Statistics is a way to ask questions, explore, and make sense of the world around us.

The Framework for Statistical Reasoning should be used in all grade levels and courses to guide learners through the sense-making process, ultimately leading to the goal of statistical literacy in all grade levels and courses. Reasoning with statistics provides a context that necessitates the learning and application of a variety of mathematical concepts.

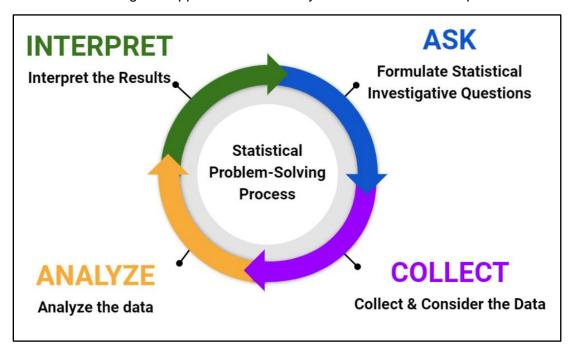


Figure 1: Georgia Framework for Statistical Reasoning

The following four-step statistical problem-solving process can be used throughout each grade level and course to help learners develop a solid foundation in statistical reasoning and literacy:

I. Formulate Statistical Investigative Questions Ask questions that anticipate variability.

II. Collect & Consider the Data

Ensure that data collection designs acknowledge variability.

III. Analyze the Data

Make sense of data and communicate what the data mean using pictures (graphs) and words. Give an accounting of variability, as appropriate.

IV. Interpret the Results

Answer statistical investigative questions based on the collected data.